

# CS249: ADVANCED DATA MINING

## Text Data: Word Embedding

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# Announcements

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- Homework 3 due today
  - Due May 10<sup>th</sup> (11:59pm)
  
- Midterm Exam
  - In class May 15<sup>th</sup>
  - Closed-Book Exam, no cell phone
  - Bring a simple electronic calculator
  - You can bring an A4 size reference sheet

# Methods Learnt: Last Lecture


	Vector Data	Text Data	Recommender System	Graph & Network
Classification	Decision Tree; Naïve Bayes; Logistic Regression SVM; NN			Label Propagation
Clustering	K-means; hierarchical clustering; DBSCAN; Mixture Models; kernel k-means	PLSA; LDA	Matrix Factorization	SCAN; Spectral Clustering
Prediction	Linear Regression GLM		Collaborative Filtering	
Ranking				PageRank
Feature Representation		Word embedding		Network embedding

# Methods to Learn

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Feature Representation		<b>Word embedding</b>		Network embedding

# Text Data: Word Embedding

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- Introduction to Word Representation 
- Word2vec: CBOW and Skip-Gram
- GloVe: Global Vectors for Word Representation
- Summary

# Why Word Representation?

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- Finding Synonyms: words that have the same meaning
  - E.g., movie and film
- Finding polysemy: words with multiple meanings
  - E.g., light
- Document representation
  - E.g., aggregation of all the word representation

# How to Represent a Word?

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- Challenge
  - Discrete structure
- Simple representation
  - One-hot representation: a vector with one 1 and a lot of zeroes
  - E.g., Motel =

[0 0 0 0 0 0 0 0 0 0 1 0 0 0]

# Problem of One-Hot Representation

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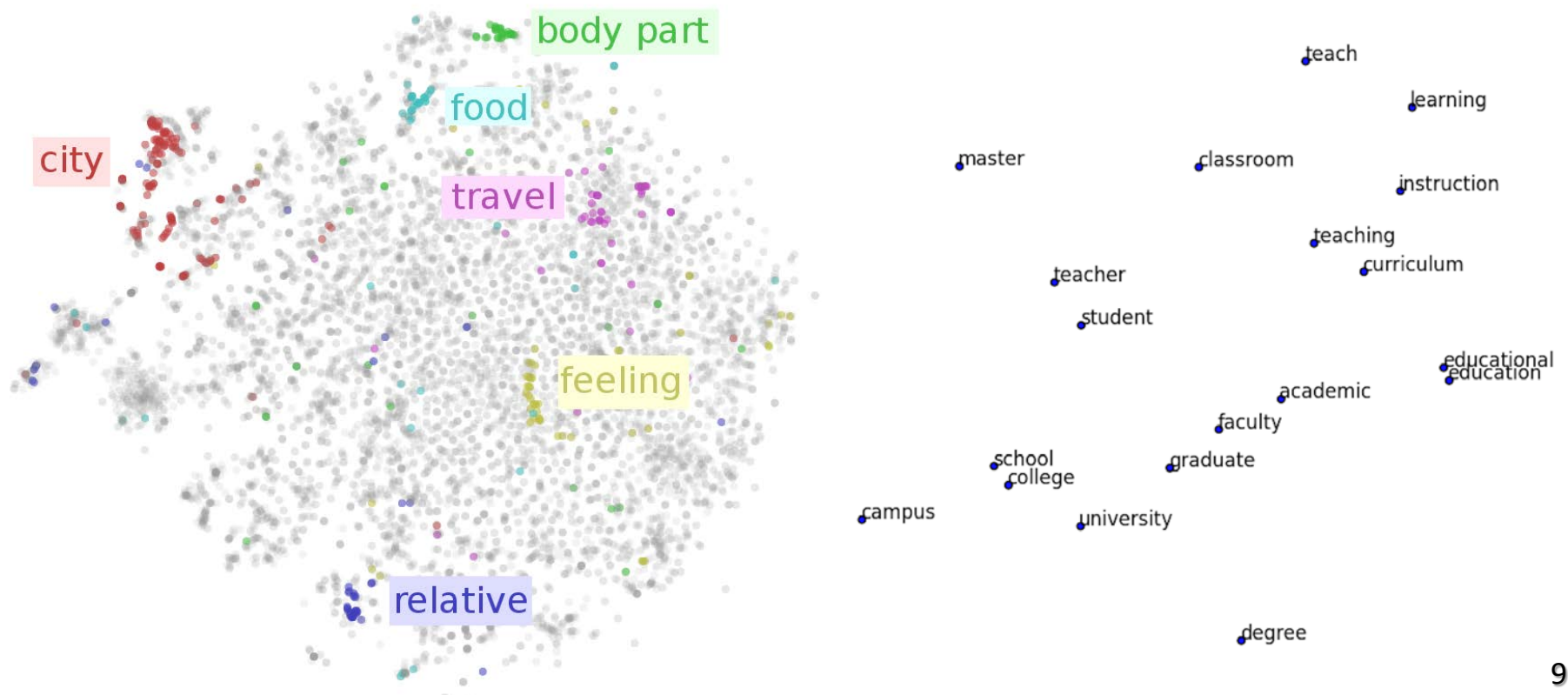
- High dimensionality
  - E.g., for Google news, 13M words
- Sparse
  - Only 1 non-zero value
- Shallow representation
  - E.g.,

motel [0 0 0 0 0 0 0 0 0 0 1 0 0 0 0] AND  
hotel [0 0 0 0 0 0 0 1 0 0 0 0 0 0 0] = 0



# Word Embedding

- Low dimensional vector representation of every word
  - E.g., motel = [1.3, -1.4] and hotel = [1.2, -1.5]



# How to Learn Such Embeddings?

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- Using context information!


...he curtains open and the moon shining in on the barely...  
...ars and the cold , close moon " . And neither of the w...  
...rough the night with the moon shining so brightly , it...  
...made in the light of the moon . It all boils down , wr...  
...surely under a crescent moon , thrilled by ice-white...  
...sun , the seasons of the moon ? Home , alone , Jay pla...  
...m is dazzling snow , the moon has risen full and cold...  
...un and the temple of the moon , driving out of the hug...  
...in the dark and now the moon rises , full and amber a...  
...bird on the shape of the moon over the trees in front...

# A Naïve Approach

- Build a **co-occurrence matrix** for words, and apply SVD

- **Example Corpus:**

- I like deep learning.
- I like NLP.
- I enjoy flying.




counts	I	like	enjoy	deep	learning	NLP	flying	.
I	0	2	1	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
.	0	0	0	0	1	1	1	0

- **Issues:**

- Global context
- SVD is very expensive

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# Word2Vec

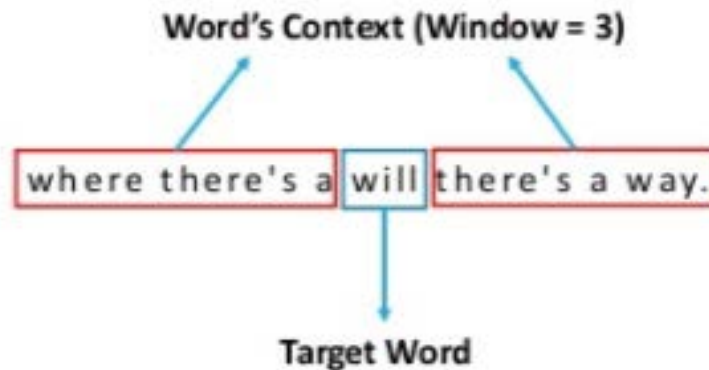
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- Proposed by Mikolov et al. at Google in 2013
- The most popular word embedding models
- Two architectures are proposed
  - Continuous bag-of-words (CBOW)
  - Skip-gram
- Extremely fast
  - “an optimized single-machine implementation can train on more than 100 billion words in one day”

# Main Idea of Word2Vec

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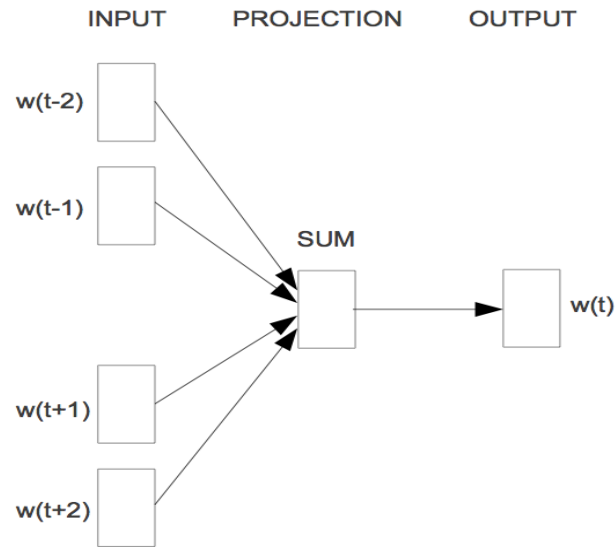
- Consider a local window of a target word



- **CBOW**: predict the target words given the neighbors
- **Skip-gram**: predict neighbors given the target words

# CBOW

- Predicting target using neighbors

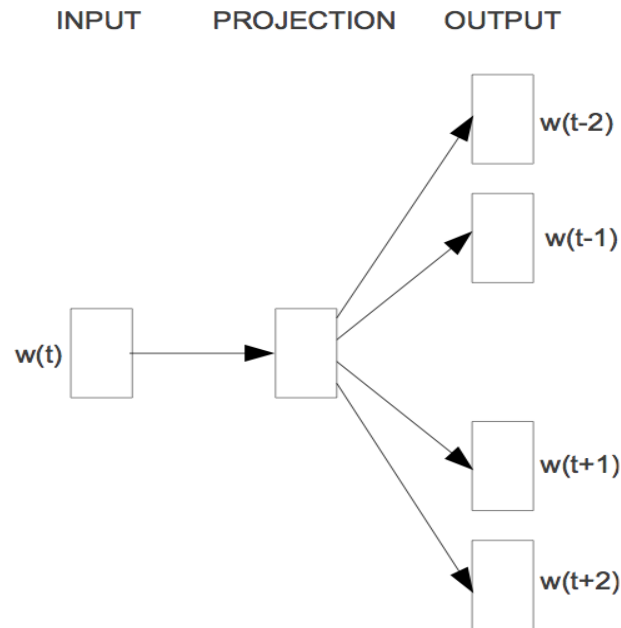


$$J_{\theta} = \frac{1}{T} \sum_{t=1}^T \log p(w_t | w_{t-n}, \dots, w_{t-1}, w_{t+1}, \dots, w_{t+n})$$

More details can be found in: [http://www.1-4-5.net/~dmm/ml/how\\_does\\_word2vec\\_work.pdf](http://www.1-4-5.net/~dmm/ml/how_does_word2vec_work.pdf)

# Skip-Gram

- Predicting neighbors using target



$$J_{\theta} = \frac{1}{T} \sum_{t=1}^T \sum_{-n \leq j \leq n, j \neq 0} \log p(w_{t+j} | w_t)$$



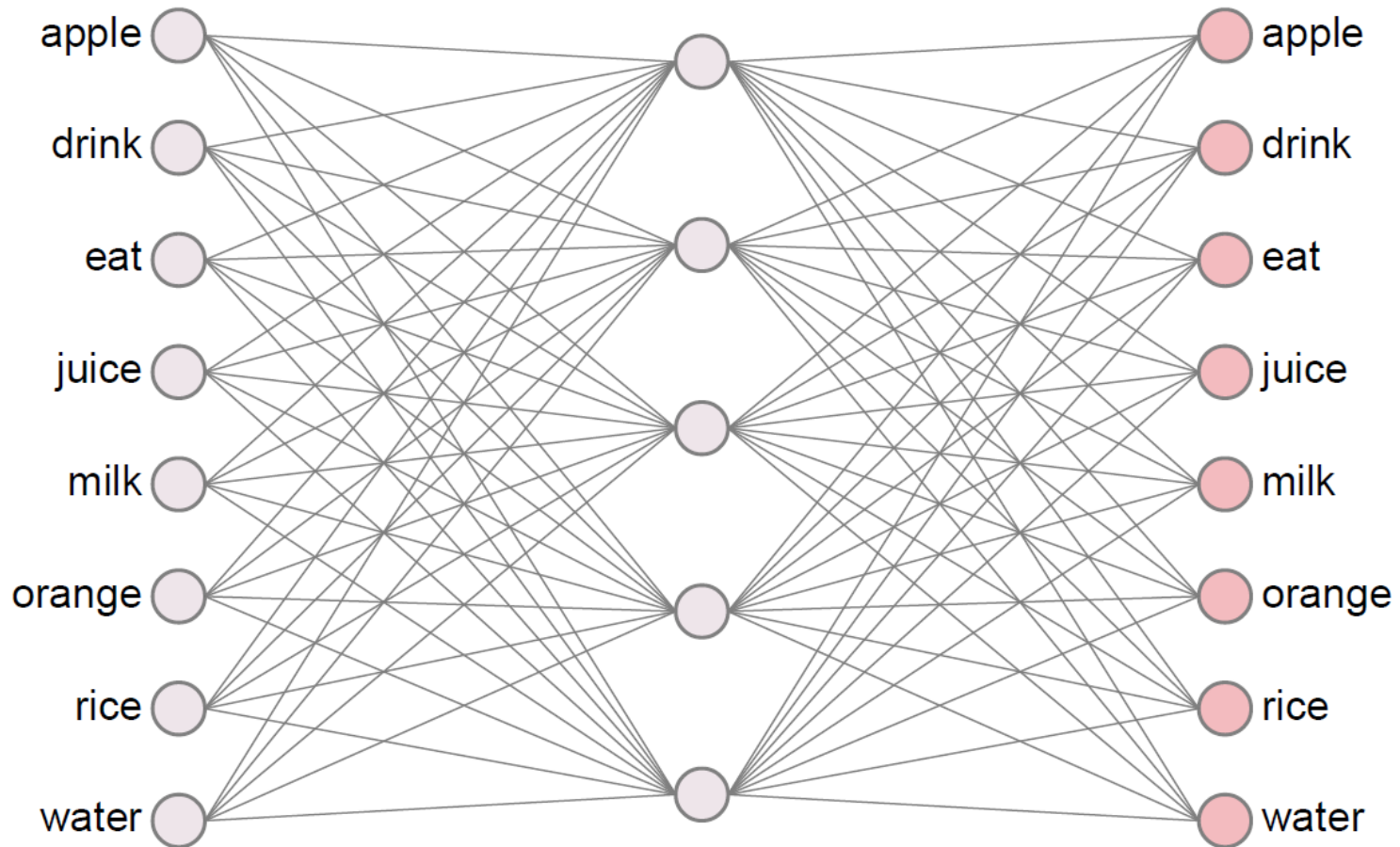
# The Conditional Probability

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- $p(w_{t+j}|w_t)$ : the probability to see  $w_{t+j}$  in target word  $w_t$ 's neighborhood
  - Intuition:  $w_t$ 's embedding should be closer to  $w_{t+j}$ 's embedding
  - Every word has two copies of embedding
    - One serves as the role of target ( $\mathbf{v}$ ), and the other serves as the role of context ( $\mathbf{u}$ )

$$p(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)}$$

# A Neural Network Point of View



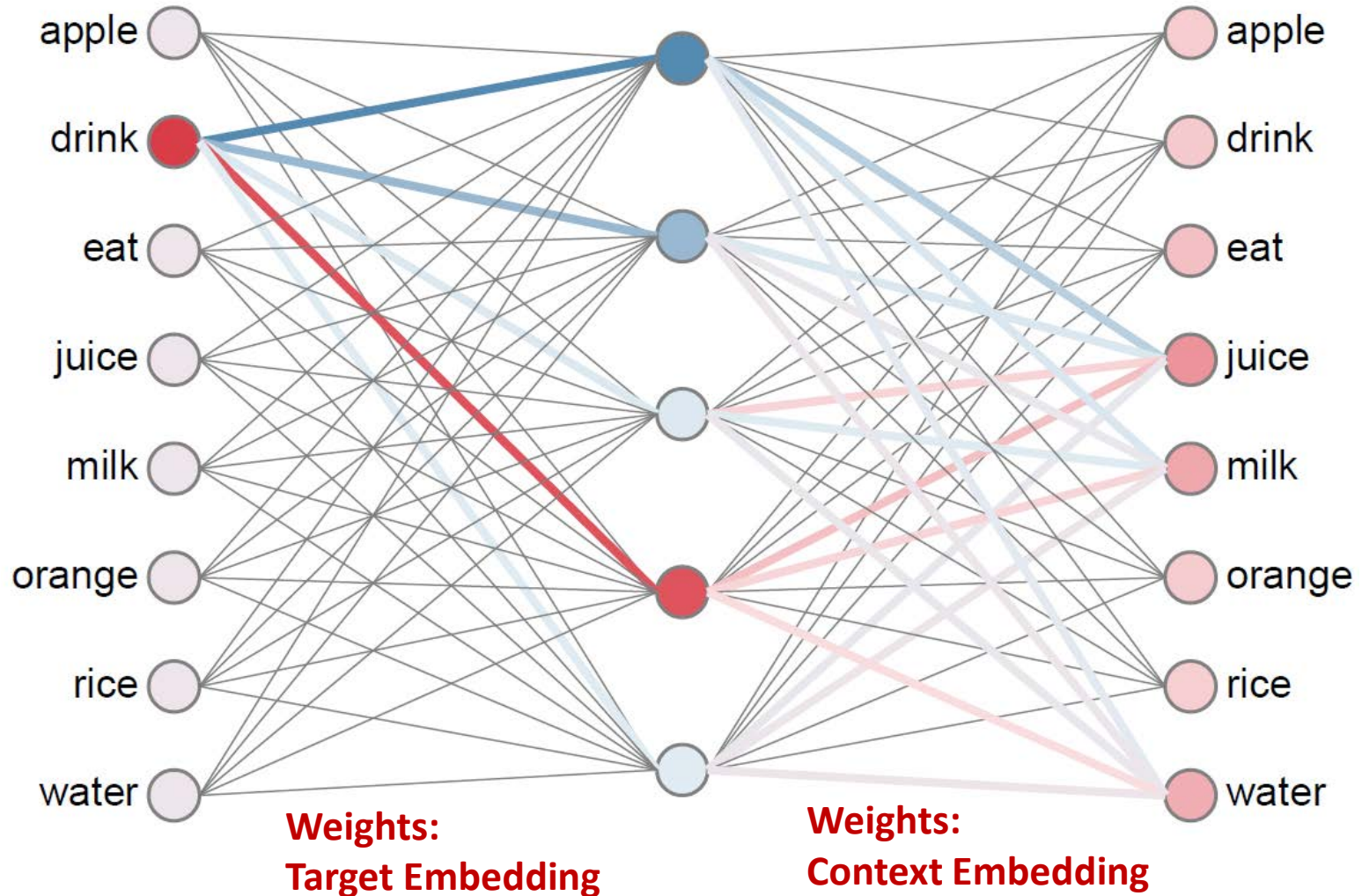
**Input Layer:**  
**one-hot vector**

**Hidden Layer:**  
**Linear (Identity)**

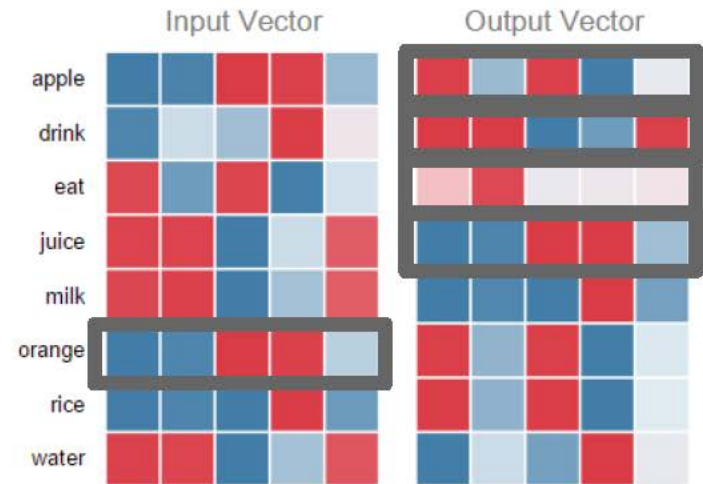
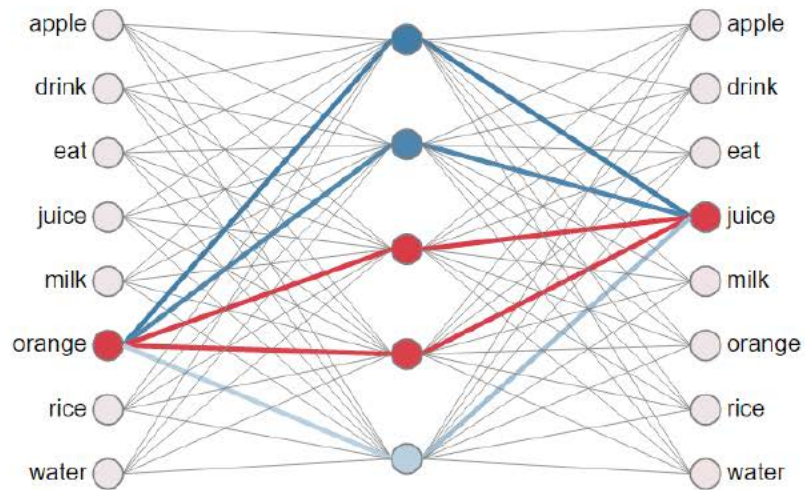
**Output Layer:**  
**softmax**

# Demo

- <https://ronxin.github.io/wevi/>

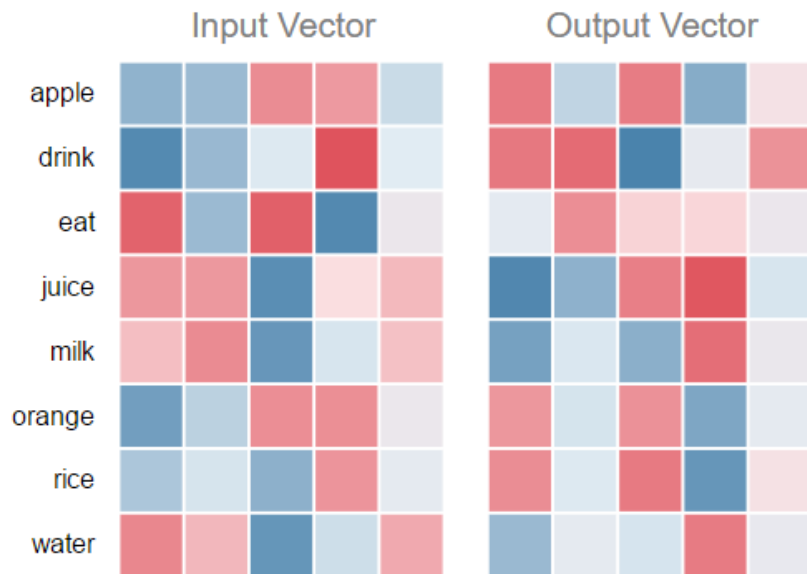


# Embedding vs. NN Weights

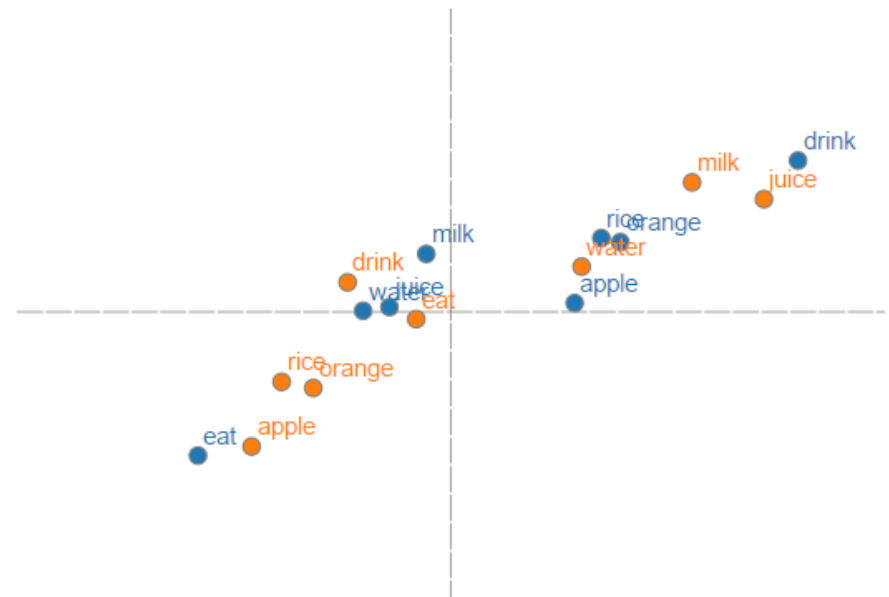


# Embedding Visualization

Weight Matrices



Vectors



# Negative Sampling for Skip-Gram

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- The original objective is not scalable for large size vocabulary!

$$p(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w=1}^W \exp(u_w^T v_c)}$$

- For each target, for every positive word, sample  $k$  negative words

$$\log \sigma(u_{w_o}^T v_{w_c}) + \sum_{i=1}^k E_{w_i \sim \underline{P_n(w)}} [\log \sigma(-u_{w_i}^T v_{w_c})]$$

$P_n(w)$ : “Negative” Distribution

# More on Negative Samples

Source Text

The quick brown fox jumps over the lazy dog. →

The quick brown fox jumps over the lazy dog. →

The quick brown fox jumps over the lazy dog. →

The quick brown fox jumps over the lazy dog. →

**Positive**

Training  
Samples

(the, quick)  
(the, brown)

(quick, the)  
(quick, brown)  
(quick, fox)

(brown, the)  
(brown, quick)  
(brown, fox)  
(brown, jumps)

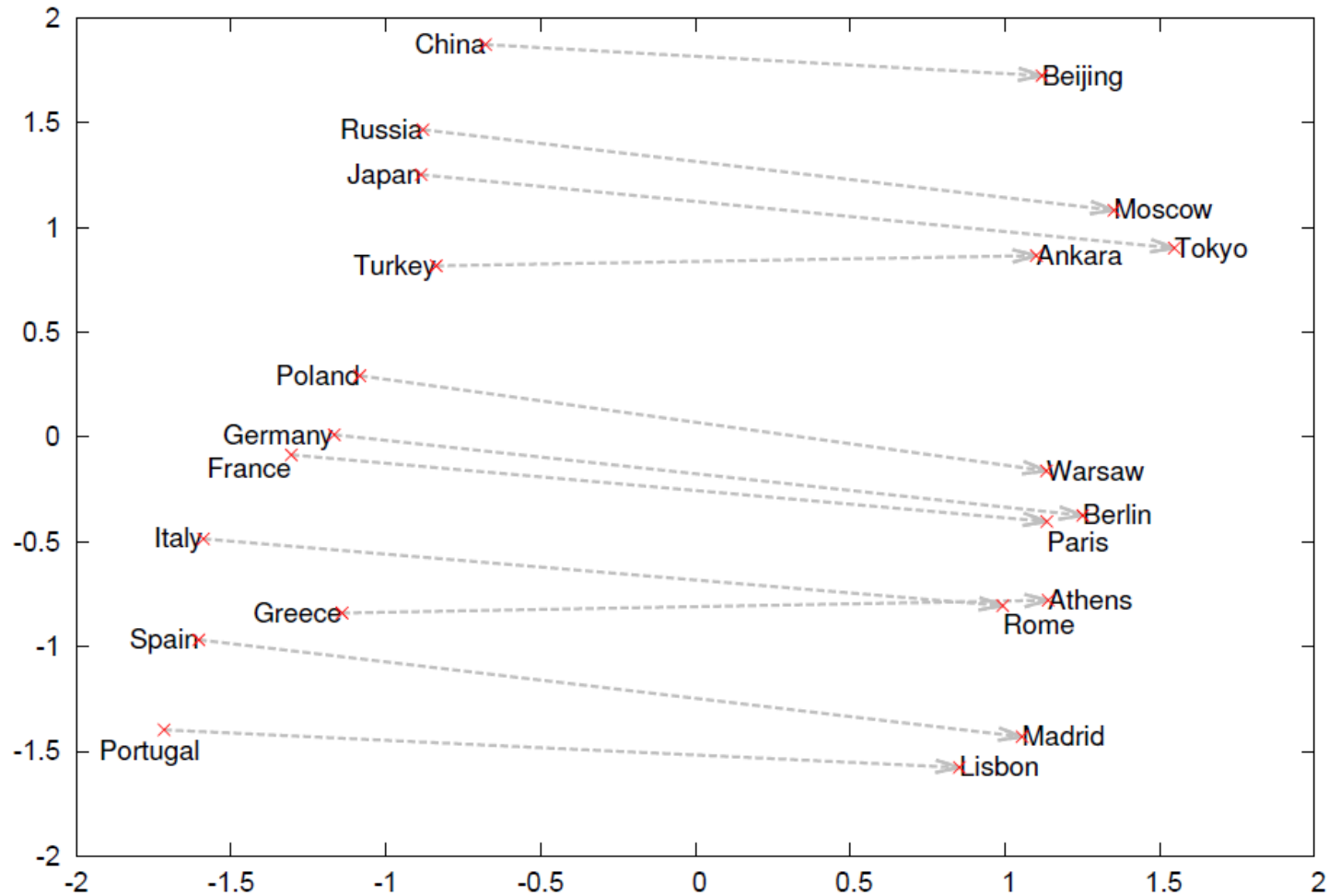
(fox, quick)  
(fox, brown)  
(fox, jumps)  
(fox, over)

**Negative, e.g., k=3**

(quick, dog)  
(quick, sky)  
(quick, flower)

# A Potential Application


- Relation detection





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# Combining Two Worlds

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- Matrix factorization for global word-word co-occurrence matrix
  - E.g., SVD
  - Global matrix factorization
- Make predictions within local context windows
  - E.g., word2vec
  - Local context window

# Objective Function

$$J = \sum_{i,j=1}^V f(X_{ij}) \left( w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij} \right)^2$$

$X_{ij}$ : number of times word  $j$  appears in the context of word  $i$

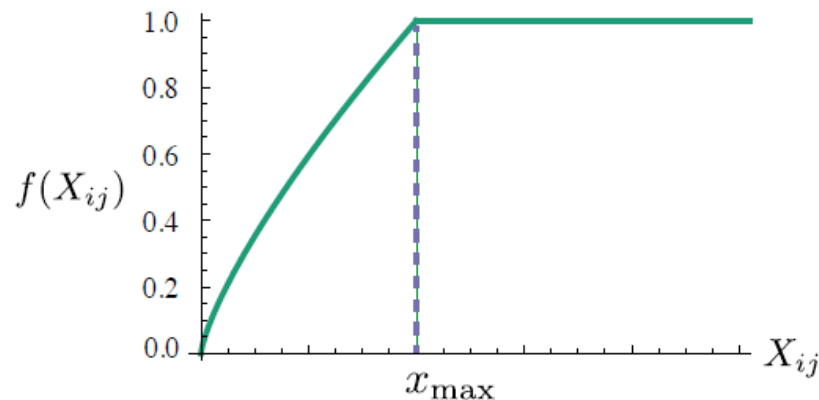
$w_i$ : word vector for word  $i$

$\tilde{w}_j$ : context word vector for word  $j$

$b_i$ : bias term for word  $i$

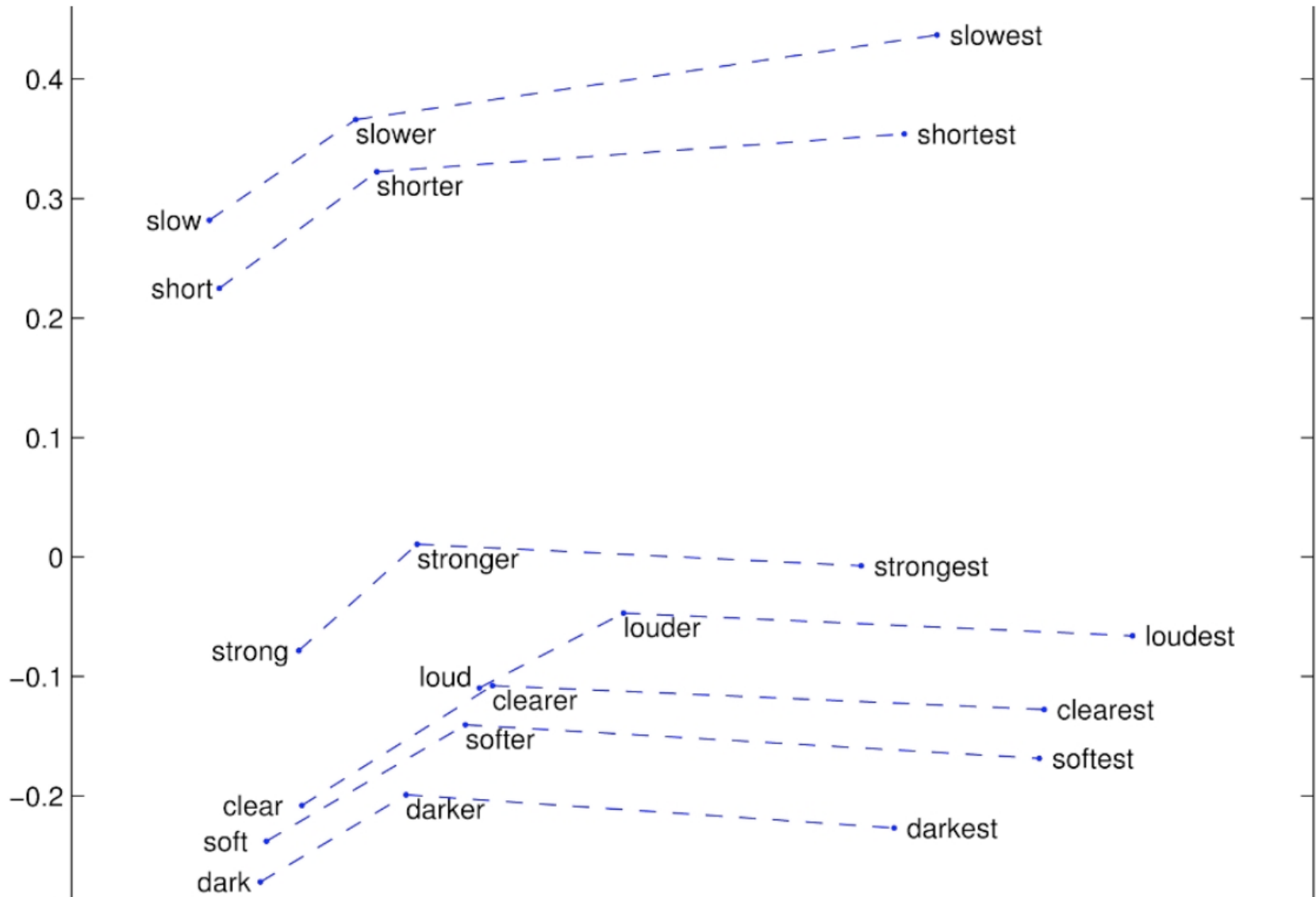
$\tilde{b}_j$ : bias term for context word  $j$

$f(X_{ij})$ : a weighting function to punish high frequencies



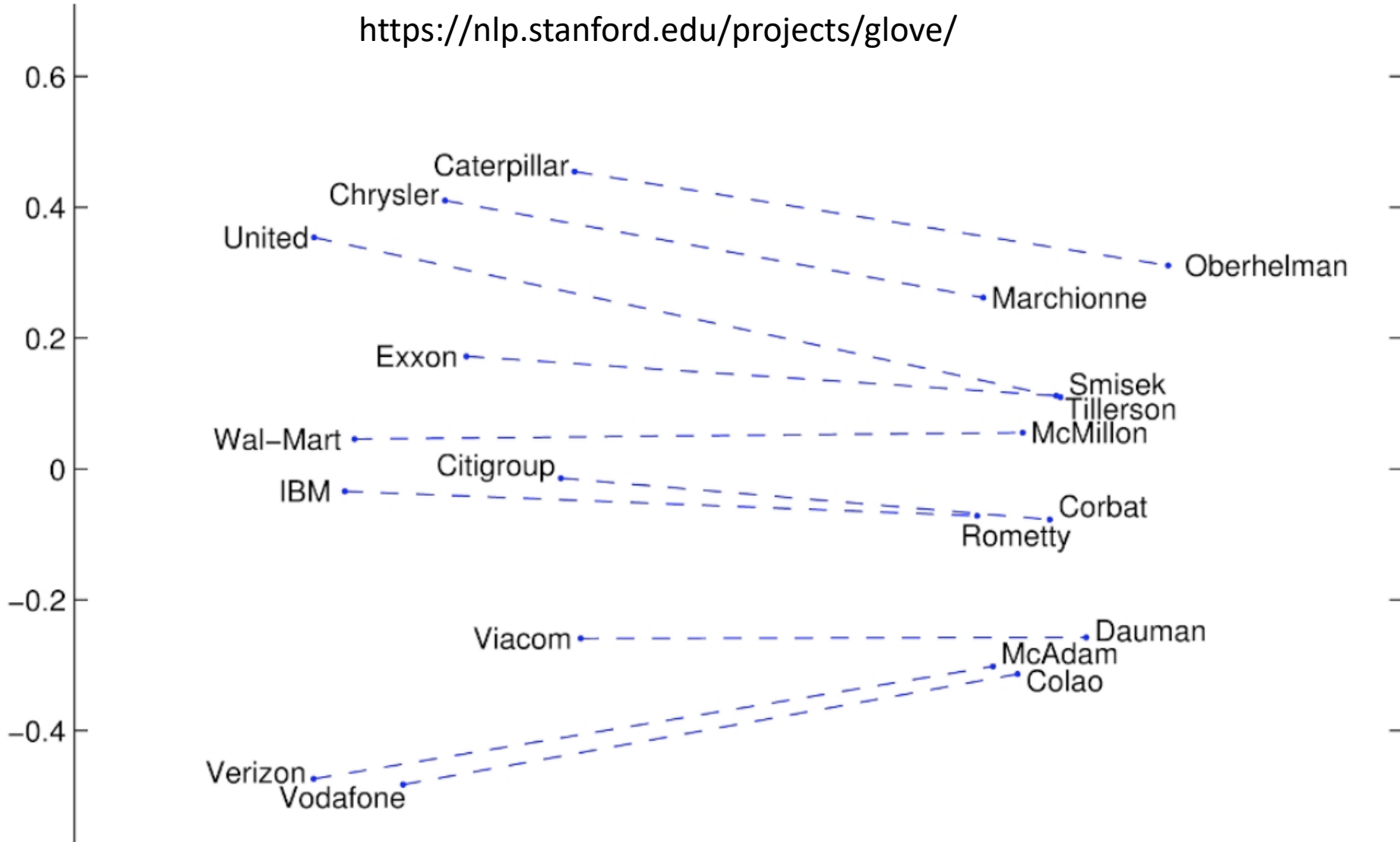
$$f(x) = \begin{cases} (x/x_{\max})^\alpha & \text{if } x < x_{\max} \\ 1 & \text{otherwise} \end{cases}$$

# Some Interesting Results: Superlatives




# Some Interesting Results: Company-CEO

<https://nlp.stanford.edu/projects/glove/>



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# Summary

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- Word embedding
  - A low-dimensional vector representation for words
- Word2vec
  - Local context-based prediction: CBOW and Skip-Gram
- Glove
  - Matrix decomposition on local context co-occurrence matrix

# References

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- Mikolov, T., Corrado, G., Chen, K., & Dean, J. (2013). Efficient Estimation of Word Representations in Vector Space. Proceedings of the International Conference on Learning Representations (ICLR 2013), 1–12.
- Mikolov, T., Chen, K., Corrado, G., & Dean, J. (2013). Distributed Representations of Words and Phrases and their Compositionality. NIPS, 1–9.
- Pennington, J., Socher, R., & Manning, C. D. (2014). Glove: Global Vectors for Word Representation. Proceedings of the 2014 Conference on Empirical Methods in Natural Language Processing, 1532–1543.